

Half Yearly Examinations for Secondary Schools 2020

YEAR 10

MATHEMATICS
Main Paper

TIME: 1h 40min

Question	1	2	3	4	5	6	7	8	9	10	Total Main	Non Calc	Global Mark
Mark													

DO NOT WRITE ABOVE THIS LINE

Name: _____

Class: _____

Calculators are allowed but all necessary working must be shown.
Answer all questions.

1.

a) Expand and simplify:

i) $4(3x - 5)$

ii) $2y(7y + 1)$

Ans: _____

Ans: _____

b) $18mn^2 = A \times 6m^2n$

Write A in terms of m and n in its simplest form.

Ans: $A =$ _____

c) Factorise completely: $12x^2y - 4xy^3$

Ans: _____

(8 marks)

2. Find the value of each letter:

a) $4^x = 16$

Ans: $x =$ _____

b) $y^3 = 27$

Ans: $y =$ _____

c) $5^a = \frac{1}{5}$

Ans: $a =$ _____

d) $19^z = 1$

Ans: $z =$ _____

(6 marks)

3. A Triathlon is a three-stage race: 1.5 km swimming, 40 km cycling and 10 km running. An athlete swam for 40 minutes, cycled for 1 hour 20 minutes and ran for 1 hour.

a) Calculate the speed for each stage of the race in km/h.

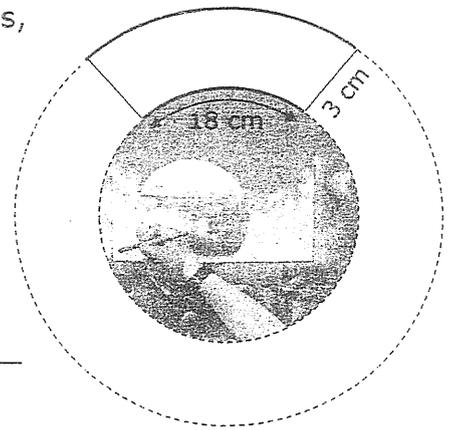
Ans: Swimming _____ ; Cycling _____ ; Running _____

b) Calculate the average speed of the Triathlon, in km/h correct to 2 decimal places.

Ans: _____

(9 marks)

4. The circular frame of a painting is made up of **six** sections, 3 cm wide. One of these sections is shown in the diagram:



- a) Calculate the circumference of the **painting**.

Ans: _____

- b) Given that $C = 2\pi r$, make r the subject of the formula.

Diagram not drawn to scale

Ans: _____

- c) Calculate the radius of the **painting**.

Ans: _____

- d) Calculate the area of the **painting**.

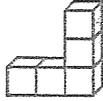
Ans: _____

- e) Calculate the area of the **frame**.

Ans: _____

(10 marks)

5. The pattern below is made of unit cubes of length 1 cm.

					
Pattern	1	2	3	4	5
Surface area (cm ²)	6	14			

a) Complete the table above.

b) What is the surface area of pattern n .

Ans: _____

c) Use your answer in question b) to find the surface area of pattern 100.

Ans: _____

d) Which pattern has an area of 254 cm²?

Ans: _____

(9 marks)

6. ABC is a straight line. ABE and BCD are two triangles such that EA is parallel to DB and EB is parallel to DC. $AB = EB$ and $\hat{BCD} = 58^\circ$

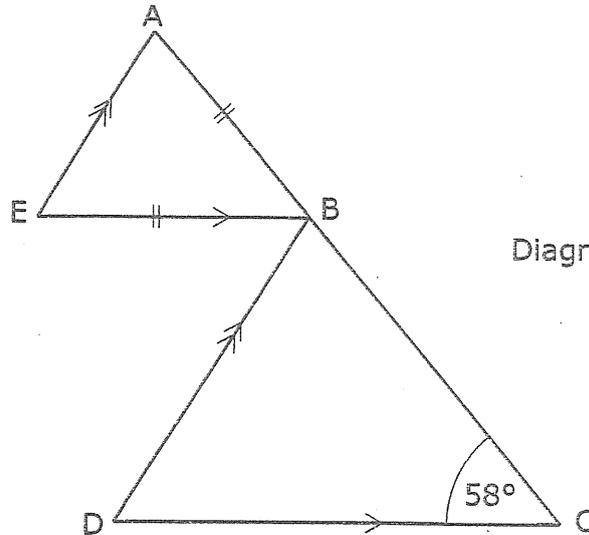


Diagram not drawn to scale

- a) Calculate the size of the following angles.
Give a reason for your answer where it is indicated.

i) \hat{ABE}

Ans: _____ Reason _____

ii) \hat{AEB}

Ans: _____

iii) \hat{BDC}

Ans: _____

iv) \hat{DBC}

Ans: _____ Reason _____

- b) What type of triangle is BDC? Give a reason for your answer.

Ans: _____ Reason _____

(10 marks)

7. A, B and C are squares drawn on the sides of a right-angled triangle.

a) What can you say about the areas of these three squares?

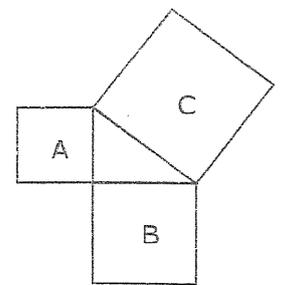


Diagram not drawn to scale

b) The area of triangle A is 3.9 cm^2 and the area of triangle B is 5.2 cm^2 .
Calculate the length of the hypotenuse of the triangle.

Ans: _____

(4 marks)

8. Ash and Smoke are two different types of grey paint. These are mixed from black and white paint in the ratios shown:

	black paint : white paint
Ash	3 : 5
Smoke	2 : 3

a) Which is the darker paint, Ash or Smoke? Show your reasoning.

b) 5 litres of black paint are used to make Smoke paint. How much white paint is needed?

Ans: _____

c) How much black paint is needed to make 2 litres of Ash paint?
Give your answer in ml.

Ans: _____

(7 marks)

9. Two trees are standing on horizontal ground. The horizontal distance between the small tree and point G on the ground is 8 m. The distance between the tops of the trees is 21 m. The angle of elevation of the tops of the trees from point G is 38° .

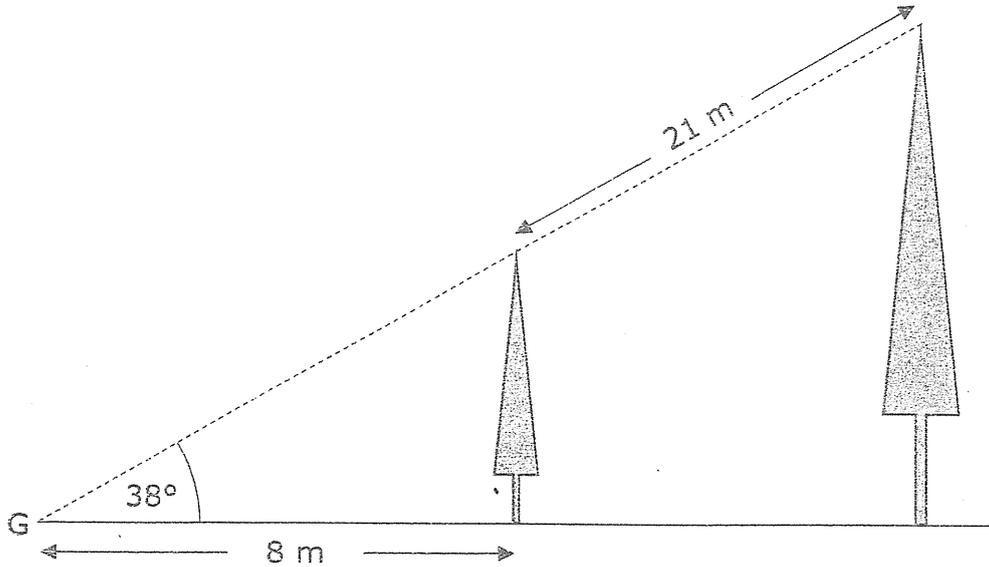


Diagram not drawn to scale

Calculate:

- a) The height of the small tree;

Ans: _____

- b) the distance between G and the top of the small tree;

Ans: _____

- c) the horizontal distance between the trees;

Ans: _____

(9 marks)

10. A traffic policeman measured the speeds of vehicles that passed on a main road. The frequency table shows all the speeds measured.

Speed (s) in km/h	$20 < s \leq 30$	$30 < s \leq 40$	$40 < s \leq 50$	$50 < s \leq 60$	$60 < s \leq 70$	$70 < s \leq 80$
Frequency	4	12	18	32	8	2

- a) Draw a histogram to illustrate the data in the frequency table.

- b) How many vehicles were moving at 40 km/h or less?

Ans: _____

- c) The speed limit for this road is 60 km/h.
How many vehicles were caught over-speeding?

Ans: _____

- d) The fines for over-speeding are:
€32 for speeds above 60 km/h up to 70 km/h;
€68 for speeds above 70 km/h up to 80 km/h;
€100 for speed above 80 km/h.

Calculate the total amount of fines in euro.

Ans: _____

(8 marks)

End of examination